

# Pre-Calculus: Sec. 5.5 (Day 1)

## Solving Trigonometric Equations Strategies:

- 1) Need the same angle (argument): ex.  $x$ ,  $2x$ ,  $3x$ ,  $x/2$ , etc...
- 2) Try to get the **same function** if it will help.
- 3) Look for rules/identities.
- 4) Beware of the “temptation”: ex.  $\sin x \tan x = \sin x$   
(Do Not Divide out a trig. function!!!)
- 5) If you have a **MULTIPLE** angle: ex.  $2x$ ,  $3x$ ,  $x/2$ , etc...  
substitute in  $\theta$ , solve, then substitute back.
- 6) Graphing calculator. Calculate intersections or zeros, depending on what you input.

# Beware!!!

When solving trigonometric equations you sometimes will need to check for **extraneous solutions**.

- 1) Whenever you square both sides of the equation (or raise both sides to any even # power) check **ALL** solutions. Actually plug each answer into the original equation and check if the value works, for each angle found.
- 2) If the original equation has  $\tan x$ ,  $\cot x$ ,  $\sec x$  or  $\csc x$  (which means any function other than  $\sin x$  or  $\cos x$ ) **and** the answer is a **quadrantal angle**. Only check the quadrantals because they may be undefined. (You do not need to do this for  $\sin x$  and  $\cos x$  because they are never undefined).

1) Find all solutions (also known as general solutions) of the equation, in radians. (No calculator)

$$\sin x = -\frac{\sqrt{3}}{2}$$

2) Find all solutions of the equation, in radians. (No calculator)

$$\tan x = -\frac{\sqrt{3}}{3}$$

3) Find all solutions of the equation, in radians. (No calculator)

$$\sqrt{2}\sin x + 3 = 2$$

4) Solve on the interval  $[0, 2\pi)$

(No calculator)

(Also known as principal solutions).

$$2 \sin \theta - \csc \theta = 1$$

5) Solve on the interval  $[0, 2\pi)$ . (No calculator)

$$\sin x \tan x = \sin x$$

6) Solve on the interval  $[0, 2\pi)$ . (No calculator)

$$\sin^2 x - \cos^2 x = 0$$



- 7) Solve:     a) For principal solutions on the interval  $[0, 2\pi)$ .  
                  b) For general solutions.

$$2 \sin^2 x - 1 = -\sin x$$

- 8) Solve:     a) For principal solutions on the interval  $[0, 2\pi)$ .  
                  b) For general solutions.

$$\cos^2 x + 2 \sin x = -2$$