Hyperbola: Sec. 9.2

General Form:

$$Ax^2 + Bx - Cy^2 + Dy + E = 0$$

 $\frac{(x-h)^2}{a^2} - \frac{(y-k)^2}{b^2} = 1 \quad \leftarrow \text{This must be equal to } 1.$ Standard

form:

The x^2 portion is positive, so the hyperbola crosses over the x-axis. Transverse axis is horizontal.

center: (h, k)

The line segment connecting the vertices is the transverse axis. The foci are c units from the center,

where
$$c^2 = a^2 + b^2$$

Asymptotes :
$$y = k \pm \frac{b}{a}(x-h)$$

Hyperbola: Sec. 9.3

Form:

form:

 $Ay^2 + By - Cx^2 + Dx + E = 0$ General $\frac{(y-k)^2}{a^2} - \frac{(x-h)^2}{b^2} = 1 \quad \leftarrow \text{This must be equal to } 1.$ **Standard** The y^2 portion is positive, so the hyperbola crosses over the y-axis.

Transverse axis is vertical.

center: (h, k)

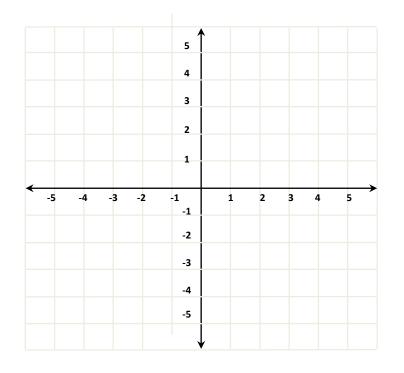
The line segment connecting the vertices is the transverse axis. The foci are c units from the center,

where $c^2 = a^2 + b^2$

Asymptotes :
$$y = k \pm \frac{a}{b}(x-h)$$

Ex. 1) Find the standard form of the equation, the center, vertices, foci, and asymptotes of the hyperbola. Then sketch the hyperbola, labeling these parts.

$$x^2 - 9y^2 + 36y - 72 = 0$$



Ex. 2) Find the standard form of the equation, the center, vertices, foci, and asymptotes of the hyperbola. Then sketch the hyperbola, labeling these parts. $9y^2 - 4x^2 - 18y + 24x - 63 = 0$

