

Pre-Calculus: Sec. 1.3 The Difference Quotient

Ex1) *Given*: $f(x) = 2x^2 - x + 3$

Find the Difference Quotient (simplified) : $\frac{f(x+h) - f(x)}{h}; h \neq 0$

Ex2) *Given*: $f(x) = \sqrt{x}$

Find the Difference Quotient (simplified) : $\frac{f(4+h) - f(4)}{h}; h \neq 0$

Ex3) Given: $f(x) = x^3 - 8x$

Find the Difference Quotient (simplified): $\frac{f(x+h) - f(x)}{h}; h \neq 0$

Sec. 1.3 Even or Odd Functions

To Determine Even or Odd Functions...

- Always find $f(-x)$ first!!! Then...

If $f(-x) = f(x)$:

(Same as Original)

Then the function is **Even**

The graph of an Even function has y -axis symmetry.

(both $(-x, y)$ and (x, y) are on the graph)

If $f(-x) = -f(x)$:

(Opposite of the Original)

Then the function is **Odd**

The graph of an Odd function has origin symmetry.

(both (x, y) and $(-x, -y)$ are on the graph)

Find the coordinates of a 2nd point on
the graph:

Given:

Even Function

Odd Function

$(-2, 3)$

$(6, -1)$

$(-5, -2)$

Ex. 1: Algebraically determine whether each of the following functions are even, odd, or neither.

$$a) h(x) = \frac{-x}{\sqrt{7+x^2}}$$

$$b) f(x) = \frac{x-1}{x-2x^2}$$

$$c) g(x) = 2x|x^2 - 3|$$

$$d) f(x) = -2x^3 - x + 3$$

$$e) r(x) = \frac{3x^2 - 7}{|x| + 5}$$

Review: Find the domain for the following functions.

Express your answers in *set* and *interval* notation.

$$a) f(x) = \sqrt{49 - x^2}$$

$$b) g(x) = \frac{2x}{\sqrt{x-3}}$$

$$c) h(x) = \frac{3x}{\sqrt{x^2 + 2}}$$

$$d) k(x) = 2 + \log_5(x-1)$$

$$e) f(x) = \frac{-7x}{\log_3(x-5)}$$