## Pre-Calculus

Sec. 4.3
Right Triangle Trig.

## Ex.1) Find the value of $\cos \theta$ and $\tan \theta$, if $\theta$ is an angle in the

 $3^{\text {rd }}$ quadrant, and $\sin \theta=-\frac{5}{8}$.Ex.2) Find the exact value of the unknown variables in the right triangle.


## Cofunction Rules

Sine and Cosine Secant and Cosecant Tangent and Cotangent Ex. $\sin 30^{\circ}=1 / 2=\cos 60^{\circ}$
This occurs because the angles are complementary, in general, it can be shown from the right triangle definitions that cofunctions of complementary angles are equal.
(The angles add up to $90^{\circ}$ or $\pi / 2$.)

## Cofunction Identities

$$
\begin{array}{ll}
\sin \left(90^{\circ}-\theta\right)=\cos \theta & \cos \left(90^{\circ}-\theta\right)=\sin \theta \\
\tan \left(90^{\circ}-\theta\right)=\cot \theta & \cot \left(90^{\circ}-\theta\right)=\tan \theta \\
\sec \left(90^{\circ}-\theta\right)=\csc \theta & \csc \left(90^{\circ}-\theta\right)=\sec \theta
\end{array}
$$

For radians $\pi / 2$ will be substituted for $90^{\circ}$.

Note: These equations move from both left to right and right to left. Expand and Condense!!!!

Ex3) Find a cofunction with the same value as the given expression.
a) $\sin 35^{\circ}$
b) $\tan \frac{2 \pi}{11}$
c) $\sec 17^{\circ}$

## Ex4) Evaluate with a calculator (Round to 4 decimal places.)

a) $\tan 35^{\circ}$ b) $\cot 35^{\circ}$
c) $\csc 5$
d) $\cot \frac{7 \pi}{5}$

Ex5) Use a calculator to find the value of the acute angle $\theta$ in radians, round to 3 decimal places. a) $\sin \theta=0.9499$
b) $\tan \theta=0.5117$

Ex.6) A girl flies a kite with a 100 foot string. The angle of elevation of the string is $52^{\circ}$. How high off the ground is the kite? Round answer to 3 decimal places.


Ex. 7) An airplane takes off 200 yards in front of a 60 foot building. At what angle of elevation must the plane take off in order to avoid crashing into the building? Assume that the airplane flies in a straight line and the angle of elevation remains constant until the airplane flies over the building. Round answer to 3 decimal places.


Ex.8) Find each value of $\theta$ in degrees $\left(0^{\circ}<\theta<90^{\circ}\right)$ and radians $\left(0<\theta<\frac{\pi}{2}\right)$ without a calc.
a) $\cot \theta=\frac{\sqrt{3}}{3}$
b) $\sec \theta=\sqrt{2}$

Ex.9) Evaluate:
a) $\tan \frac{\pi}{4}+\csc \frac{\pi}{6}$
b) $6 \tan \frac{3 \pi}{4}+\sin \frac{\pi}{3} \sec \frac{\pi}{6}$

